

Lectures 5-6

Imperative languages

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Literature

- Textbooks:
 - John Mitchell, Concepts in Programming Languages, Cambridge Univ Press, 2003 (Chapters 5 and 8)
 - Michael L. Scott, Programming Language Pragmatics (3rd ed.), Elsevier, 2009 (Chapters 6 and 8)
- Many examples are from:
 - Emmanuel Chailloux, Pascal Manoury, Bruno Pagano, Developing Applications With Objective Caml, English translation, O'REILLY, 2000

Outline

- Introduction
- Memory and variables
- Sequences, conditional statements and blocks
- Loops
- Procedures and functions
- Records
- Pointers
- Arrays
- Sets, unions, dictionaries

Functional vs. imperative approach

- Functional programming
 - Abstract computation model is λ -calculus
 - Program is a function represented by a λ -term,
 - The outcome is obtained by its reduction
 - Functions do not have side effects
 - Variables outside the function can not be altered
- Imperative programming
 - Abstract computation model is a Turing machine
 - Program is a sequence of instructions
 - Program has states; results are computed by executing instructions
 - Instructions change the state of main memory
 - The outcome is obtained when the final state is reached

Imperative programming

- Early imperative programming languages
 - Fortran, 1954; mathematical formulas
 - Still popular programming language
 - BASIC, 1960; Beginners' All-purpose Symbolic Instruction Code
 - Pascal, 1970; Algorithms + Data Structures = Programs
 - C, 1972; Constructs map efficiently to typical machine instructions
 - January 2021, C was ranked first in the TIOBE index
 - On top of lists: on demand, job offers, Web search results
 - Fortran is still among the most popular languages for numeric processing

Example

Let us compute the greatest common divisor of two integers

OCaml

```
let rec gcd x y =  
  if y = 0 then x  
  else gcd y (x mod y);;
```

Functional: values, recursion

Imperative: variables, loops, sequences

C

```
int gcd(int x, int y) {  
  while (y != 0) {  
    int t = x % y;  
    x = y; y = t;  
  }  
  return x;  
}
```

Structured control

- Structured programming, 1970
 - Emerged in late 1950s with ALGOL 58, ALGOL 60
 - Coined by Edsger W. Dijkstra
 - Paper “Go To Statement Considered Harmful”, open letter, 1968
 - Structured and unstructured control flow
 - Unstructured: GOTO statements
 - Structured: syntactical constructs direct computation
 - »Revolution« in software engineering
 - Top-down design (i.e., progressive refinement)
 - Modularization of code
 - Structured types (records, sets, pointers multidim. arrays)
 - Descriptive variable and constant names
 - Extensive commenting conventions

Structured control

- Strong influence on imperative programming languages
 - Most structured programming ideas were implemented in imperative languages
 - Pascal, C, Modula, Ada, Oberon, Java, C#, ...
 - But also in ML, Scala, F#, ...
- Most of modern algorithms can be elegantly expressed in imperative languages
 - All classical algorithms implemented in imperative languages (Dijkstra, Floyd, Knuth, ...)

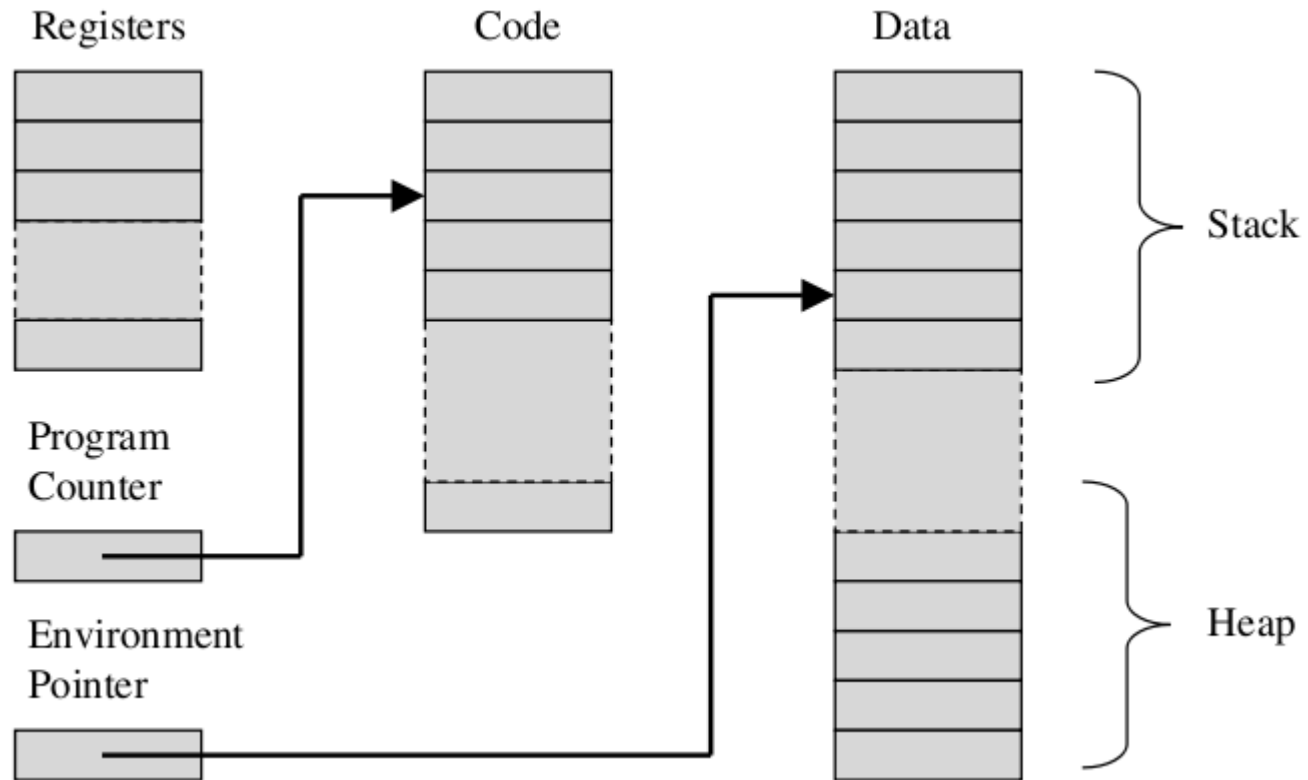
Concepts of imperative languages

- Read-write memory, variables
- Instructions and sequences of instructions
- Blocks
- Conditional statements
- Loops - conditional loops, iterations through ranges or through containers
- Procedures and functions
- Records and arrays
- Sets, unions and dictionaries

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Program memory



Variables

- Memory of a program is organised into memory cells
- Any cell can be accessed via its address; an integer, usually in range $0 - (2^{62} - 1)$
- Variable is a symbolic name for a memory space of given size
 - Variable can be accessed by using the name instead of the address of the memory cell
- Namespaces in a program
 - A program context (block, function, module)
 - A namespace includes information about variables
 - Name (identifier), the address of the beginning of memory space, the size of allocated memory
 - Namespaces are often organized hierarchically

Operations with variables

- Program must allocate the memory space before the variable is used
 - The allocation can be either static or dynamic
- Program reads the contents of the memory in the moment we refer to the identifier (name)
- The contents of the memory referred by a variable is changed by assignment
- The variable is freed either on the end of execution or on demand
- Possible problems:
 - Read/write unallocated memory, concurrent write, memory leak
 - We will study these problems in lecture on memory management

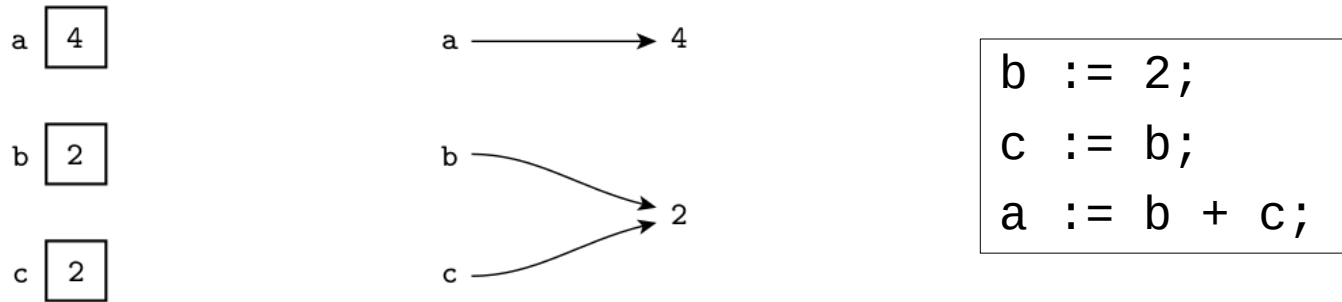
Models of variables

- Two models of variables
 - Value model and reference model
- Value model of variables
 - Variable is a named container for a value
 - Location and value (see variable a)
 - l-value = refers to the location of a variable (left-hand side of assignment statements)
 - r-value = refers to the value of a variable (expressions that denote values)
 - both l-values and r-values can be complicated expressions
 - An expression can be either an l-value or an r-value, depending on the context
 - C, C++, Pascal, Ada, Java (simple values), etc.

```
d = a;  
a = b + c;
```

Models of variables

- Reference model of variables



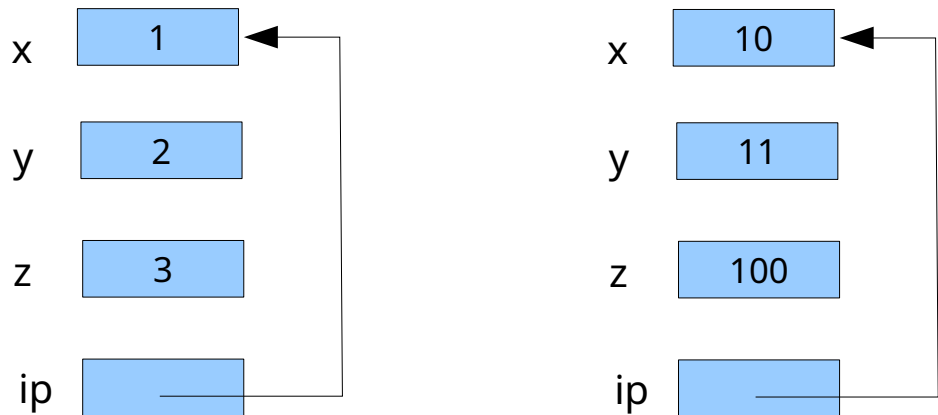
- A variable is a named reference to a value
 - every variable is an l-value
 - variable in a context of an r-value must be dereferenced
 - dereference is automatic in most PL but not in ML
- Reference model is (not) more expensive
 - Use multiple copies of immutable objects
- Algol68, Clu, Lisp/Scheme, Python, ML, Haskell, and Smalltalk

Variables in C

- Two important operators
 - Operator `>>&<<`: returns address of variable
 - Operator `>>*<<`: returns value of variable (from an address)

```
int x = 1, y = 2, z = 3;  
int *ip;  
ip = &x;  
y = *ip;  
*ip = 0;  
*ip = *ip + 10;  
y = *ip + 1;  
z = *ip * 10;
```

Value model

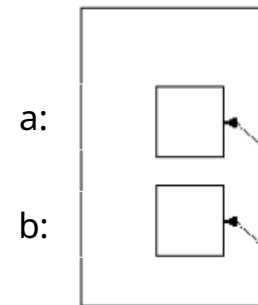


Two important operators

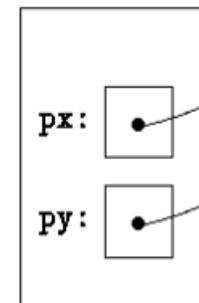
- Operator `>&<<`: returns address of variable
- Operator `>*<<`: returns value of a variable

```
swap(&a, &b);  
...  
void swap(int *px, int *py) {  
    int temp;  
    /* interchange *px and *py */  
    temp = *px;  
    *px = *py;  
    *py = temp;  
}
```

in caller:



in swap:

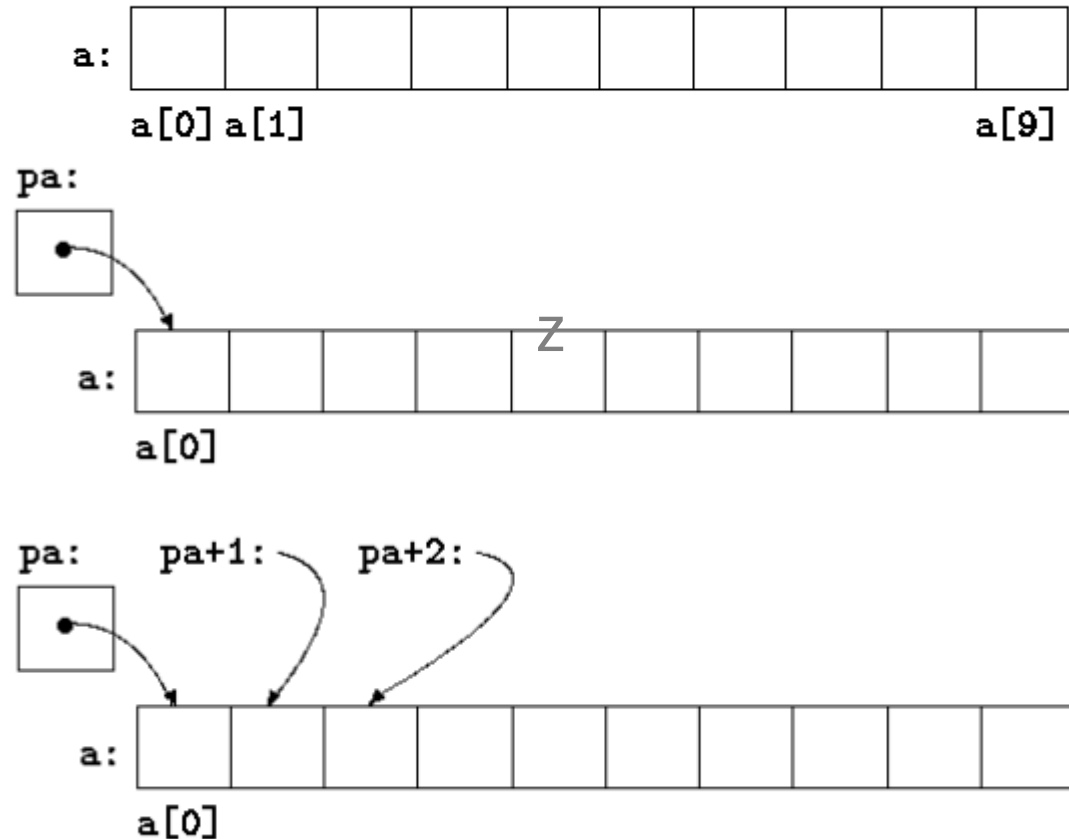


Pointers and arrays in C

- C has pointer arithmetic

```
int a[10];  
// a[0], a[1],..., a[9]  
pa = &a[0];
```

```
/* strlen: return length of string s */  
int strlen(char *s) {  
    int n;  
    for (n = 0; *s != '\0', s++)  
        n++;  
    return n;  
}
```



Variables in OCaml

```
type 'a ref = {mutable contents: 'a}
```

- Variables are implemented by using a reference type
- OCaml has weaker, but safer model of a variable
 - Reference is initialised on creation by the referenced value
 - Memory space is automatically allocated using the type of referenced value
 - Assignment is a special function with resulting type unit
 - The result of reading has the type of referenced variable
- Drawbacks of the model
 - Functions cannot be referenced
 - We do not have full access to the program's memory – no pointers, no pointer arithmetic

Examples of variables in Ocaml

<pre># let x = ref 2 ;;</pre>	(* declaration and allocation
<pre>val x : int ref = {contents=2}</pre>	
<pre># !x;;</pre>	(* reading, notice operator '!'
<pre>- : int = 2</pre>	
<pre># x ;;</pre>	(* reading of the reference
<pre>- : int ref = {contents=2}</pre>	
<pre># x := 5; !x;;</pre>	(* assignment
<pre>- : int = 5</pre>	
<pre># x := !x * !x; !x;;</pre>	(* reading, operation, and assignment
<pre>- : int = 25</pre>	
<pre># let l = ref [1;2;3];;</pre>	
<pre>val l : int list ref = {contents = [1; 2; 3]}</pre>	
<pre># !l;;</pre>	
<pre>- : int list = [1; 2; 3]</pre>	
<pre># l := 0::!l; !l;;</pre>	
<pre>- : int list = [0; 1; 2; 3]</pre>	

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Sequence

- Sequence is fundamental abstraction used to describe algorithms
 - Von Neumann's instruction cycle

```
LOOP: execute *PC;    // execute instruction referenced by PC
      PC++;           // increment program counter (PC) by 1
      goto LOOP;      // loop
```

- Sequence of instructions change the state of variables (memory)

```
int t = x % y;
x = y;
y = t;
```

Sequences in OCaml

- Syntax of OCaml sequences

```
let t = ref 0
and x = ref 42
and y = ref 28 in begin
  t:= !x mod !y;
  x:=!y;
  y:=!x ;
end;;
```

`<expr1>; <expr2>; <expr3> (* list of exprs *)`

- Every expression in a sequence must be of type `unit`.

```
# print_int 1; 2; 3;;
Warning 10: this expression should have type unit.
1- : int = 3
```

```
# print_int 2; ignore 4; 6;;
2- : int = 6
```

Blocks

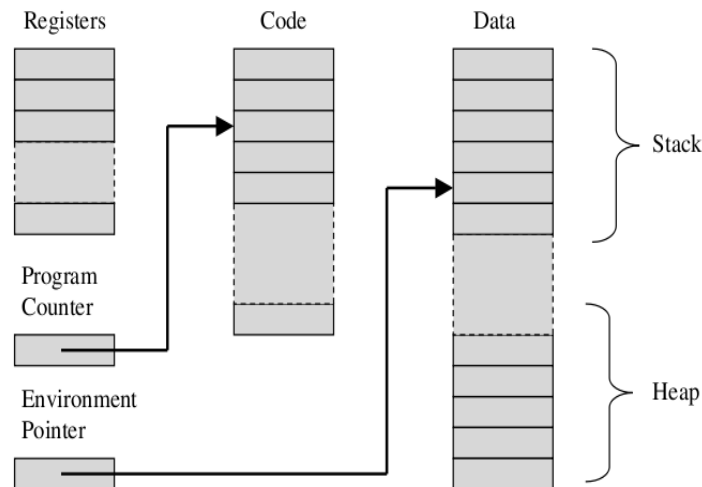
- Imperative languages are typically block-structured languages
- Block is a sequence of statements enclosed by some structural language form
 - Begin-end blocks, loop blocks, function body, etc.

```
begin
  let t = ref 0
  and x = ref 42
  and y = ref 28 in
  begin
    t:= !x mod !y;
    x:=!y;
    y:=!x;
  end;
end;;
```

```
outer { {int x = 2;
block { { int y = 3; } inner
      { x = y+2; } block
      }
}
```


Blocks

- Each block is represented using activation record
 - Includes parameters and local variables
 - Includes memory location for return value
 - Includes control pointers to be detailed in next lectures
 - Control pointers are used to control computation
- Activation records are allocated on program stack
 - Presented in lecture on Memory management



Conditional statements

- Machine languages use instructions for conditional jumps
 - Initial imperative approach
- OCaml syntax

```
if <cond_expr> then <expr_true> else <expr_false> ;;
```

- Conditional statements is a concept shared between imperative and functional languages
 - Both branches must agree on type in Ocaml
 - Conditional statement in Ocaml has value

```
# (if 1 = 0 then 1 else 2) + 10;;  
- : int = 12
```

JE/JZ	Jump if equal/Jump if zero
JNE/JNZ	Jump if not equal/Jump if not zero
JA/JNBE	Jump if above/Jump if not below or equal
JAE/JNB	Jump if above or equal/Jump if not below
JB/JNAE	Jump if below/Jump if not above or equal
JBE/JNA	Jump if below or equal/Jump if not above
JG/JNLE	Jump if greater/Jump if not less or equal
JGE/JNL	Jump if greater or equal/Jump if not less
JL/JNGE	Jump if less/Jump if not greater or equal
JLE/JNG	Jump if less or equal/Jump if not greater
JC	Jump if carry
JNC	Jump if not carry

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Loops – while-do

- Repeat a block of commands while (or until) a condition is satisfied
 - Loop body changes the state of program
- Statement `while` in OCaml

```
while <cond_expr> do
  <sequence>
done
```

```
# let gcd (x,y) =
  let t = ref 0 in
  while !y != 0 do
    t := !x mod !y; x := !y; y := !t
  done; !x;;

val gcd : int ref * int ref -> int = <fun>
# let a = ref 42 and b = ref 28;;
val a : int ref = {contents = 42}
val b : int ref = {contents = 28}
# gcd (a,b);;
- : int = 14
# (!a,!b);;    (* passing references! *)
- : int * int = (14, 0)
```

Loops – for statement

- Statement for is classical construct of imperative programming languages
- Statement for in OCaml

```
for <sym> = <exp1> to <exp2> do
    <exp3>
done
for <sym> = <exp1> downto <exp2> do
    <exp3>
done
```

```
/* atoi: convert s to integer */
int atoi(char s[])
{
    int i, n, sign;
    for (i = 0; isspace(s[i]); i++) ;    /* skip white space */
    sign = (s[i] == '-') ? -1 : 1;
    if (s[i] == '+' || s[i] == '-') i++; /* skip sign */
    for (n = 0; isdigit(s[i]); i++)      /* convert s to integer */
        n = 10 * n + (s[i] - '0');
    return sign * n;
}
```

- Used in
 - Imperative
 - Script
 - OO
 - Modular programming languages

Ocaml: for->while statement

```
let is_digit = function '0' .. '9' -> true | _ -> false;;  
let is_white = function ' ' | '\n' | '\t' -> true | _ -> false;;
```

```
let int_of_string s =  
  begin  
    let i = ref 0 and n = ref 0 in  
    while is_white(s.[!i]) do i := !i+1; done;  
    let sign = (if s.[!i]='-' then -1 else 1) in  
    if s.[!i]='+' || s.[!i]='-' then i := !i+1;  
    while is_digit(s.[!i]) do  
      n := 10 * !n + (int_of_char(s.[!i]) - int_of_char('0'));  
      i := !i+1;  
    done;  
    sign * !n;  
  end;;
```

```
# let s = "-12\n";;  
val s : string = "-12\n"  
# int_of_string s;;  
- : int = -12
```

Loops – do-while statement

- Loop condition is at the end of loop block
 - do-while syntax in C prog. lang. (also in Java)
 - Not included in Ocaml!

```
do <sequence>
while <cond_expr>
```

- repeat-until in Pascal
- Example:
 - Kernighan & Ritchie: The C programming language

```
/* itoa: convert n to characters in s */
void itoa(int n, char s[]) {
    int i, sign;
    if ((sign = n) < 0) /* record sign */
        n = -n;        /* make n positive */
    i = 0;
    do { /* generate digits in reverse order */
        s[i++] = n % 10 + '0'; /* get next digit */
    } while ((n /= 10) > 0); /* delete it */
    if (sign < 0)
        s[i++] = '-';
    s[i] = '\0';
    reverse(s);
}
```

Ocaml: do-while->while statement

```
let string_of_int n =  
  begin  
    let s = Bytes.make 10 ' ' and sign = n and nr = ref n and i = ref 0 in  
    if sign < 0 then nr := -n;  
    Bytes.set s !i (char_of_int(!nr mod 10 + int_of_char('0')));  
    nr := !nr / 10;  
    while (!nr > 0) do  
      i := !i + 1;  
      Bytes.set s !i (char_of_int(!nr mod 10 + int_of_char('0')));  
      nr := !nr / 10;  
    done;  
    if (sign < 0) then begin i := !i + 1; Bytes.set s !i '-'; end;  
    reverse(Bytes.to_string (Bytes.trim s));  
  end;;
```


Loop control

- Loop control in C programming language
 - Jumping out of a loop – break
 - Jumping to a loop condition – continue
 - Not included in Ocaml!

```
for (i = 0; i < n; i++)  
    if (a[i] < 0)  
        /* skip negative elements */  
        continue;  
...  
    /* do positive elements */
```

- Kernighan & Ritchie:
The C programming
language

```
/* trim: remove trailing blanks, tabs, newlines */  
int trim(char s[]) {  
    int n;  
    for (n = strlen(s)-1; n >= 0; n--)  
        if (s[n] != ' ' && s[n] != '\t' && s[n] != '\n')  
            break;  
    s[n+1] = '\0';  
    return n;  
}
```

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Procedures and functions

- Abstraction is a process by which the programmer can associate a symbol or a pattern with a programming language construct.
 - Control and data abstractions
- Subroutines are the principal mechanism for control abstraction.
 - Part of program with well defined input and output is abstracted as subroutine, procedure, or function.
 - Subroutine performs operation on behalf of caller.
 - Caller passes arguments to subroutine by using parameters
 - Subroutine that returns values is a function.
 - Subroutine that does not is called a procedure.

Procedures and functions

- Most subroutines have parameters
- Procedure was first abstraction in Algol-family of programming languages

- Formal and actual parameters of procedure

```
procedure Proc(First : Integer; Second: Character);  
Proc(24,'h');
```

- Actual parameters are mapped to formal parameters
- The most common parameter-passing modes
 - Some languages define a single set of rules that apply to all parameters (C, Java, Fortran, ML, and Lisp)
 - Others have more modes of parameter passing (Pascal, C++, Ada, ...)

Parameter passing

- Input and output of procedure is realized by means of parameter passing

- Passing values

- C (only cbv), Java, Ocaml, C++, Pascal, ...

- Passing references

- Pascal, C++, Fortran, ...

```
Procedure Square(Index : Integer;  
                Var Result : Integer);  
  
  Begin  
    Result := Index * Index;  
  End
```

- Other parameter passing issues

- Passing structured things

- arrays, structures, objects

- Missing and default parameters

- Named parameters

- Variable-length argument lists

Passing values

- The most commonly used method
 - Values of actual parameters are copied to formal parameters
 - Java uses only this method (arrays and structures are identified by references)
- Parameter is seen as local variable of procedure
 - It is initialized by the value of actual parameter

Java

```
int plus(int a, int b) {  
    a += b;  
    return a;  
}  
  
int f() {  
    int x = 3; int y = 4;  
    return plus(x, y);  
}
```

Ocaml

```
# let plus ((a:int), (b:int)) : int = a + b;;  
val plus : int * int -> int = <fun>  
# let f () =  
    let x = 3 and y = 4  
    in plus (x,y);;  
val f : unit -> int = <fun>  
# f ();;  
- : int = 7
```

Passing references

- Reference to variable is passed to procedure
 - Code of procedure is changing passed variable
 - All changes are retained after the call
 - Passed variable and formal parameter are aliases
- Best method for larger structures!

C

```
void plus(int a, int *b) {  
    *b += a;  
}  
...  
int x = 3;  
plus(4, &x);  
// x == 7  
...
```

Ocaml

```
# let plus ((a:int), (b:int ref)) : unit =  
    b := a + !b;;  
val plus : int * int ref -> unit = <fun>  
# let a = 4 and b = ref 3;;  
val a : int = 4  
val b : int ref = {contents = 3}  
# plus (a,b);;  
- : unit = ()  
# !b;;  
- : int = 7
```

Variations on value and reference parameters

- C++ references

- In C++, C references are made explicit
- C++ implements call-by-reference

```
void swap(int &a, int &b) { int t = a; a = b; b = t; }
```

- Call-by-sharing

- Barbara Liskov, CLU (also Smalltalk)
- Objects (identifiers) are references
- No need to pass reference (to references)
- Just pass reference

Variations on value and reference parameters

- Call-by-value/Result
 - Actual params are copied to formal params initially
 - Result is copied back to actual parameter before exit
- Read-only parameters
 - Modula-3 provided read-only params
 - Parameter values can not be changed
 - Read-only params are available also in C (const)
- Parameters in Ada,
 - Modes: in, out, in out (also in PL/SQL)
 - Named parameters / position parameters

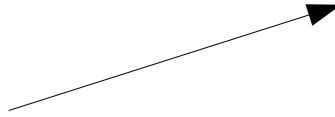
Variations on value and reference parameters

- Default values of parameters
 - Ada, Oracle PL/SQL
- Variable length argument lists
 - Programming language C, Perl, ...
 - No type-checking, no control, may be dangerous

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Type declaration

- Type is defined from simpler types
 - By using **type constructors**
 - *, |, record, list, array, ...
- Type definition in Ocaml 
- No parametrized (polymorphic) types in imperative languages!
 - Just concrete
- **Records, Pointers and Arrays !**
 - Types of imperative programming languages
 - Presented in this section

```
type name = typedef ;;  
type name1 = typedef1  
and name2 = typedef2  
...  
and namen = typedefn ;;
```

Records

- Record types allow related data of heterogeneous types to be stored and manipulated together.
- Records in programming languages
 - Originally introduced by Cobol
 - In Algol 68 called them structures (also in C)
 - They use the keyword `struct`
 - Later in Fortran 90 they named them *record type*
 - In C++ structures are special form of a class
 - Java has no notion of a structure
 - C# and Swift use reference model for classes and value model for the type `struct` (no inheritance)

Records

- In C, a simple record might be defined as follows:
- Each of the record components is known as a field.
- To refer to a given field of a record, most languages use “dot” notation:

```
struct element {  
    char name[2];  
    int atomic_number;  
    double atomic_weight;  
    _Bool metallic;  
};
```

```
element copper;  
const double AN = 6.022e23;    /* Avogadro's number */  
...  
copper.name[0] = 'C'; copper.name[1] = 'u';  
double atoms = mass / copper.atomic_weight * AN;
```

Records in Ocaml

- Record is a product with named components
- Record type definition and record constr. in Ocaml

```
type name = { name1 : t1 ; . . . ; namen : tn }  
            { name1 = expr1 ; . . . ; namen = exprn }
```

- Record components can be defined mutable
 - Component assignment operation

```
type name = { ...; mutable namei: ti ; ... }
```

```
expr1.name <- expr2
```

```
# type complex = { mutable re:float;  
                   mutable im:float } ;;  
type complex = { mutable re : float;  
                 mutable im : float; }  
# let c = {re=2.;im=0.} ;;  
val c : complex = {re=2; im=0}
```

```
# c.im <- 3.;;  
- : unit = ()  
# c;;  
- : complex = {re = 2.; im = 3.}  
# c = {im=3.;re=3.} ;;  
- : bool = true
```

Records in Ocaml

- Operations:
 - Accessing components
 - Pattern matching

expr.name

{ name_i = p_i ; . . . ; name_j = p_j }

```
# let add_complex c1 c2 = {re=c1.re+.c2.re; im=c1.im+.c2.im};;
val add_complex : complex -> complex -> complex = <fun>
# add_complex c c ;;
- : complex = {re=4; im=6}
# let mult_complex c1 c2 = match (c1,c2) with
({re=x1;im=y1},{re=x2;im=y2}) -> {re=x1*.x2-.y1*.y2; im=x1*.y2+.x2*.y1} ;;
val mult_complex : complex -> complex -> complex = <fun>
# mult_complex c c ;;
- : complex = {re=-5; im=12}
```


Example in Ocaml

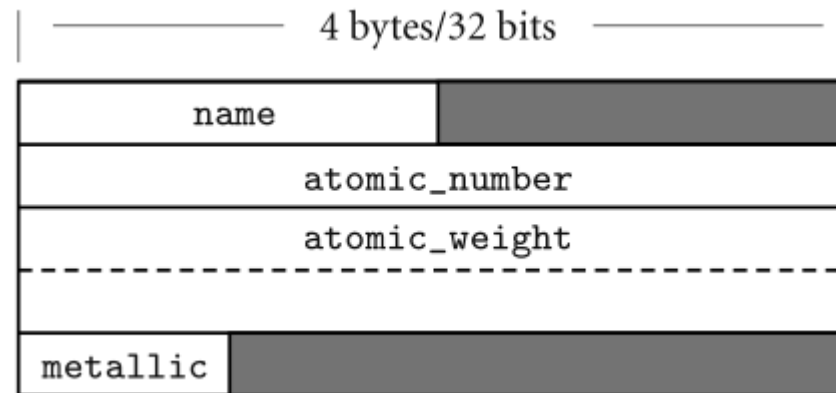
```
# type point = { mutable xc : float; mutable yc : float } ;;
type point = { mutable xc: float; mutable yc: float }
# let p = { xc = 1.0; yc = 0.0 } ;;
val p : point = {xc=1; yc=0}
# p.xc <- 3.0 ;;
- : unit = ()
```

```
# let moveto p dx dy =
  begin
    p.xc <- p.xc +. dx;
    p.yc <- p.yc +. dy;
  end;;
val moveto : point -> float -> float -> unit = <fun>
# moveto p 1.1 2.2 ;;
- : unit = ()
# p ;;
- : point = {xc=4.1; yc=2.2}
```

Memory layout for records

- The fields of a record are usually stored in adjacent locations in memory.
- Compiler keeps track of the offset of each field within each rec. type.
- Value model (of var.)
 - Nested records are embedded in parent record
- Reference model
 - Fields are references to in another location.

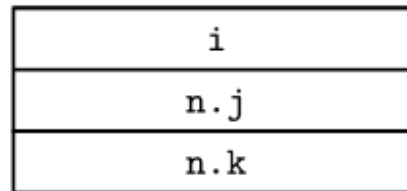
```
struct element {  
    char name[2];  
    int atomic_number;  
    double atomic_weight;  
    _Bool metallic;  
};
```



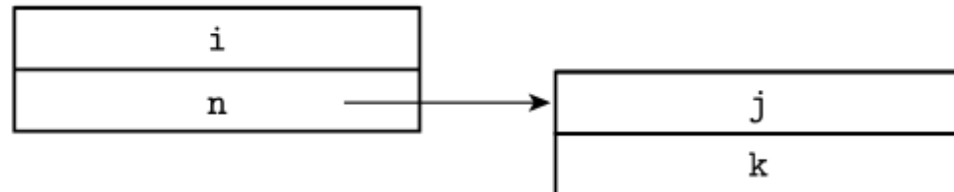
Memory layout for records

- Layout of memory for a nested struct (class) in C (top) and Java (bottom).

```
struct T {  
    int j;  
    int k;  
};  
struct S {  
    int i;  
    struct T n;  
};
```



```
class T {  
    public int j;  
    public int k;  
}  
class S {  
    public int i;  
    public T n;  
}
```



Outline

- Introduction
- Memory and variables
- Sequences, conditional statements and blocks
- Loops
- Procedures and functions
- Records
- Pointers
- Arrays
- Sets, unions, dictionaries

Pointers

- A pointer is a reference to an object in memory
 - There were attempts to call it reference
 - Pointer is usually represented by a memory address
 - A pointer can be **typed** (ML,C++,Java, ...)
 - PL then knows the structure and size of referenced object
 - The access to the object can now be checked by a compiler
 - A pointer can be **untyped** (Lisp,C)
 - Programmer must know the object pointed to by a pointer
 - Compiler does not know the structure of object
 - Therefore, it can not check the access to the object

Pointers and recursive structures

- A recursive data structure includes at least one reference to an object of the same type
 - A recursive structure can be implemented by using a structure that includes components
 - Records, products, lists, arrays and unions.
- Languages using reference model
 - Components include references to other objects
 - No need to define pointers; they are defined implicitly
- Languages using value model
 - Components must include pointers to objects and not object values

Pointers

- Pointed location
 - In some languages pointers are restricted to refer to objects on heap (Java, Pascal, Ada, Modula)
 - Object is created with operation new() that returns pointer
 - This is the only way you can create a pointer
 - Other languages use pointers that can point to any location (C, C++)
 - These languages use operator address-of '&'
- Disposing allocated objects
 - Some languages use explicit operation for releasing the allocated memory space (C, C++, Pascal)
 - Possible errors: memory leak, accessing disposed object
 - Others use automatic memory management (Java, C#)

Pointers

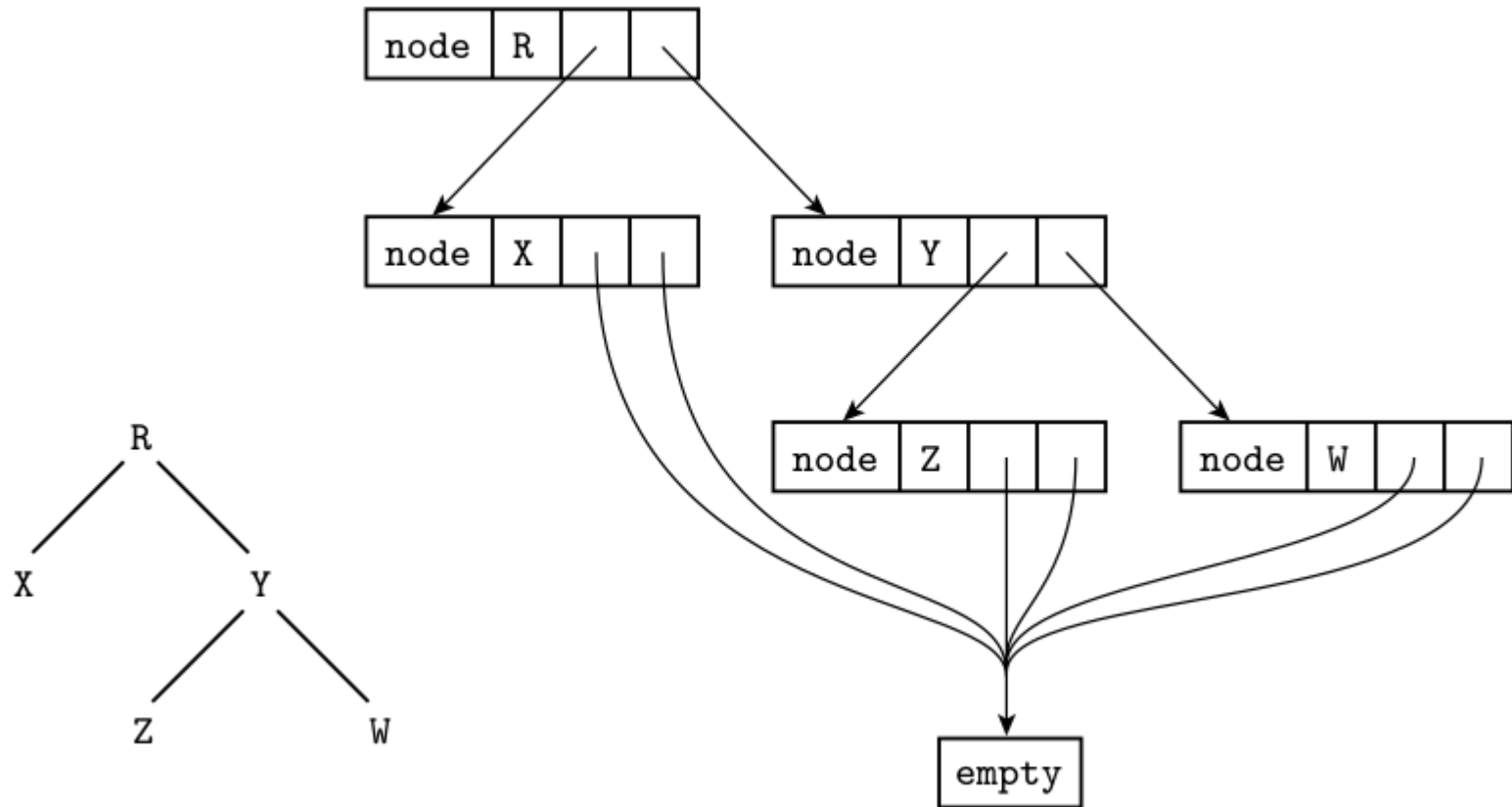
- Operations on pointers depend on the model of variables
 - Allocation and deallocation of objects on the heap
 - Reference model usually implies automatic memory management
 - Value model often implies manual storage allocation/deallocation
 - Dereferencing a pointer to access an objects to which it points
 - Need to dereference in the case of reference model
 - No need to dereference in the case of value model
 - Assignment of one pointer to another
 - In the case of a reference model, pointers are copied as references
 - In case of value model, an assignment copies the value, so the pointers have to be used

Reference model

- Recursive data structures include the pointers to structures of the same kind
- An example of a recursive data structure in **Ocaml**
 - ML uses references to identify tuples, lists, records, arrays, ...

```
# type ctree = Empty | Node of char * ctree * ctree;;  
type ctree = Empty | Node of char * ctree * ctree  
# Node('R',Node('X',Empty,Empty),  
        Node('Y',Node('Z',Empty,Empty),  
              Node('W',Empty,Empty)))
```

Recursive types in OCaml

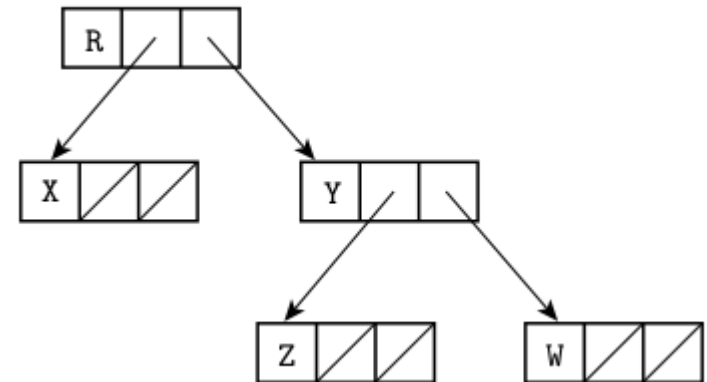


Value model

- Recursive data structures in languages with explicit pointers
 - Imperative languages with the value model of variables
 - C, C++, ML, ...
- Example in Pascal and C

```
type chr_tree_ptr = ^chr_tree;  
  chr_tree = record  
    left, right : chr_tree_ptr;  
    val : char  
  end;  
  
new(my_ptr);
```

```
struct chr_tree {  
    struct chr_tree *left, *right;  
    char val;  
};  
  
my_ptr = malloc(sizeof(struct chr_tree));
```



Example: Implementation of lists

```
# type 'a rnode = { mutable cont: 'a; mutable next: 'a rlist }  
  and 'a rlist = Nil | Elm of 'a rnode;;  
type 'a rnode = { mutable cont : 'a; mutable next : 'a rlist; }  
and 'a rlist = Nil | Elm of 'a rnode
```

```
# let l1 = Elm {cont = 1; next = Elm {cont = 2; next = Nil}};;  
val l1 : int rlist = Elm {cont = 1; next = Elm {cont = 2; next = Nil}}  
# let cons v l = Elm {cont=v; next=l};;  
val cons : 'a -> 'a rlist -> 'a rlist = <fun>
```

```
# let ( ** ) v l = cons v l;;  
val ( ** ) : 'a -> 'a rlist -> 'a rlist = <fun>  
# let l2 = cons 3 (cons 4 Nil));;  
val l2 : int rlist = Elm {cont = 3; next = Elm {cont = 4; next = Nil}}  
# let l3 = 5**6**Nil;;  
val l3 : int rlist = Elm {cont = 5; next = Elm {cont = 6; next = Nil}}
```

Example: Implementation of lists

```
# exception EmptyList;;
exception EmptyList
# let head l = match l with Nil -> raise EmptyList | Elm r -> r.cont;;
val head : 'a rlist -> 'a = <fun>
# let tail l = match l with Nil -> raise EmptyList | Elm r -> r.next;;
val tail : 'a rlist -> 'a rlist = <fun>
# head l1;;
- : int = 1
# tail l1;;
- : int rlist = Elm {cont = 2; next = Nil}
```

```
# let rec length l = match l with Nil -> 0 | Elm {next=t} -> 1+length t;;
val length : 'a rlist -> int = <fun>
# length l1;;
- : int = 2
```

Example: Implementation of lists

```
# let rec append l1 l2 = match l1,l2 with
  Elm r1,_ -> Elm {cont=r1.cont; next=append r1.next l2}
| Nil,Elm r2 -> Elm {cont=r2.cont; next=append Nil r2.next}
| Nil,Nil -> Nil;;
val append : 'a rlist -> 'a rlist -> 'a rlist = <fun>
```

```
# append l1 l2;;
- : int rlist =
Elm {cont=1; next=Elm {cont=2; next=Elm {cont=3; next=Elm {cont=4; next=Nil}}}}
# l1;;
- : int rlist = Elm {cont=1; next=Elm {cont=2; next=Nil }}
# l2;;
- : int rlist = Elm {cont=3;next=Elm {cont=4;next=Nil }}
```

Example: Implementation of lists

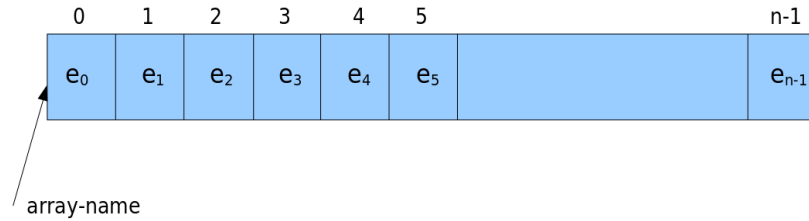
```
# let rec append1 l1 l2 = match l1 with
  Nil -> l2
| Elm r when r.next=Nil -> r.next <- l2; l1
| Elm r -> ignore (append1 r.next l2); l1;;
val append1 : 'a rlist -> 'a rlist -> 'a rlist = <fun>
```

```
# append1 l1 l2;;
- : int rlist =
Elm {cont=1; next=Elm {cont=2; next=Elm {cont=3; next=Elm {cont=4; next=Nil}}}}
# l1;;
- : int rlist =
Elm {cont=1; next=Elm {cont=2; next=Elm {cont=3; next=Elm {cont=4; next=Nil}}}}
# l2;;
- : int rlist = Elm {cont=3;next=Elm {cont=4;next=Nil}}
```

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Arrays



- Arrays are data structures holding the finite number of elements of certain data type
- Semantically, array is a mapping from an index type to a component or element type.
 - Index is usually an integer but many PLs can use discrete type
- In imperative languages an array is an important data structure
 - C, C++, Java, Fortran, Pascal, ...
 - Similar role in imperative PL as lists have in functional PL.
- An array is by definition mutable, but its size is fixed

Syntax and operations

- Accessing elements of array
 - Most languages append index delimited by a variant of parentheses to the array name (a(), a[], a{}, ...)
 - Indexes of arrays are usually of integer type but can be also of discrete type
- Declaration of an array
 - Indexes in most languages are defined by range
 - Index in C starts with 0

```
char[] upper;      /* Java */
char upper[];      /* alternative declaration */
upper = new char[26];
char upper[26];    /* C */
character, dimension (1:26) :: upper /* Fortran */
character (26) upper /* shorthand notation */
var upper : array ['a'..'z'] of char; /* Pascal */
```

Dimensions, Bounds, and Allocation

- In prev. examples, the shape of the array (including bounds) was specified in the declaration.
- For such static shape arrays, storage can be managed in the usual way
 - Static allocation for arrays whose lifetime is the entire program;
 - Stack allocation for arrays whose lifetime is an invocation of a subroutine;
 - Heap allocation for dynamically allocated arrays with more general lifetime.
- Storage management is more complex for arrays
 - Whose shape is not known until elaboration time, or
 - Whose shape may change during execution.

Dimensions, Bounds, and Allocation

- For dynamic arrays, compiler must
 - Allocate space and make shape info available at run time
 - Some PLs allow the number and bounds of dimensions to be dynamic, others allow just bounds to be dynamic
- Allocation of dynamic arrays
 - Local array may still be allocated in the stack.
 - Shape, is known at elaboration time
 - An array whose size may change is allocated in the heap.
- Descriptors, or dope vectors, hold shape information at run time
 - Offsets for record components, lower bound, the size and upper bound of each dimension
 - Dope vector may be stored in activation record on stack, or together with an array on heap

Memory Layout

- Arrays in most language implementations are stored in contiguous locations in memory.
 - One-dimensional array: one elem. after another
 - Multi-dimensional array: row-major, column-major
 - Important for nested loops to access all the elements of a large, multidimensional array.
 - Speed of such loops depends heavily effectiveness of caching
 - True multidimensional arrays use contiguous layout
- Row-Pointer Layout
 - Not stored contiguously, but in blocks including 1d arrays
 - Advantages: variable sized of rows, initialized from pieces
 - C, Ocaml, Java, C# (many provide both layouts)

```
for (i = 0; i < N; i++) {           /* rows */
    for (j = 0; j < N; j++) {       /* columns */
        ... A[i][j] ...
    }
}
```

Arrays in OCaml

```
# let v = [| 3.14; 6.28; 9.42 |] ;;  
val v : float array = [|3.14; 6.28; 9.42|]
```

- Elements can be enumerated between [|...|]
- Arrays are integrated into Ocaml
 - (but not so profoundly as lists)
- Similarly to lists, there is a module Array that includes all necessary operations
- Create an array
- Access/update an array element
 - Accessing an element
 - Setting new value

```
# let v = Array.create 3 3.14;;  
val v : float array = [|3.14; 3.14; 3.14|]
```

```
expr1.( expr2 )  
expr1.( expr2 ) <- expr3
```

Arrays in OCaml

- Example:
- Array index must not go across the borders

```
# v.(1) ;;  
- : float = 3.14  
# v.(0) <- 100.0 ;;  
- : unit = ()  
# v ;;  
- : float array = [|100; 3.14; 3.14|]
```

```
# v.(-1) +. 4.0;;
```

```
Uncaught exception: Invalid_argument("Array.get")
```

- Checking that the index is not used outside borders is **expensive**
 - Some languages do not check this by default (C)

Functions on arrays

```
# let n = 10;  
val n : int = 10  
# let v = Array.create n 0;;  
val v:int array = [|0; 0; 0; 0; 0; 0; 0; 0; 0; 0|]
```

```
# for i=0 to (n-1) do v.(i)<-i done;;  
- : unit = ()  
# v;;  
- : int array = [|0; 1; 2; 3; 4; 5; 6; 7; 8; 9|]
```

```
# let reverse v =  
  let tmp=ref 0  
  and n = Array.length(v)  
  in for i=0 to (n/2-1) do  
    tmp := v.(i);  
    v.(i) <- v.(n-i-1);  
    v.(n-i-1) <- (!tmp);  
  done;;  
- : unit = ()  
# reverse(v);;  
- : int array = [|9; 8; 7; 6; 5; 4; 3; 2; 1; 0|]
```

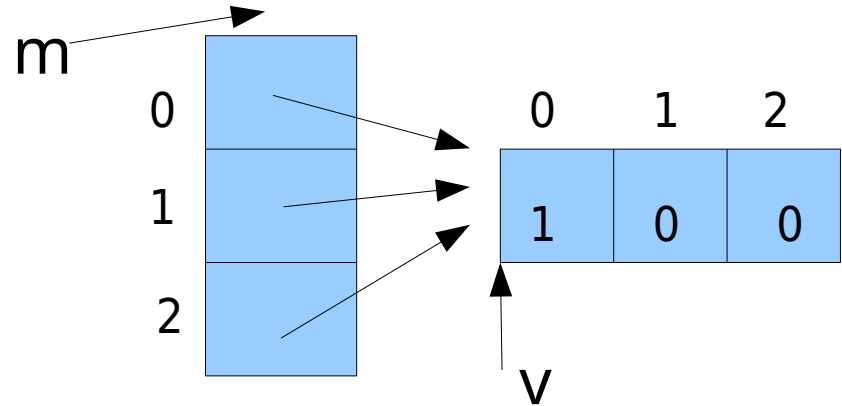
```
# let u = [|2;3|];;  
val u : int array = [|2; 3|]  
# let m = 2;;  
val m : int = 2  
# let subarray u v =  
  let found = ref false  
  and i = ref 0  
  in while ((!i<=(n-m)) && not !found) do  
    found := true;  
    for j=0 to (m-1) do  
      if v.(!i+j) != u.(j) then  
        found := false  
    done;  
    i := !i+1  
  done;  
  !found;;  
val subarray : 'a array -> 'a array -> bool = <fun>  
# subarray u v;;  
- : bool = true
```


Example: subarray()

```
# let prefix u v i =  
  let found = ref true  
  and m = Array.length(u)  
  in for j=0 to (m-1) do  
    if v.(i+j) != u.(j) then  
      found := false  
    done;  
  !found;;  
val prefix : 'a array -> 'a array -> int ->  
  bool = <fun>  
  
# prefix u v 0;;  
- : bool = false  
  
# prefix u v 2;;  
- : bool = true
```

```
# let subarray u v =  
  let found = ref false  
  and i = ref 0  
  and m = Array.length(u)  
  and n = Array.length(v)  
  in while ((!i <= (n-m)) && not !found) do  
    found := prefix u v !i;  
    i := !i+1  
  done;  
  !found;;  
val subarray : 'a array -> 'a array ->  
  bool = <fun>
```

Matrix in Ocaml is array of arrays



```
# let v = Array.create 3 0;;  
val v : int array = [|0; 0; 0|]  
# let m = Array.create 3 v;;  
val m : int array array =  
  [| [|0; 0; 0|]; [|0; 0; 0|]; [|0; 0; 0|] |]
```

```
# v.(0) <- 1;;  
- : unit = ()  
# m;;  
- : int array array =  
  [| [|1; 0; 0|]; [|1; 0; 0|]; [|1; 0; 0|] |]
```

```
# let v2 = Array.copy v ;;  
val v2 : int array = [|1; 0; 0|]  
# let m2 = Array.copy m ;;  
val m2 : int array array = [| [|1; 0; 0|]; [|1; 0; 0|]; [|1; 0; 0|] |]  
# v.(1) <- 352;;  
- : unit = ()  
# v2;;  
- : int array = [|1; 0; 0|]  
# m2 ;;
```

Matrices in Ocaml

```
# let m = Array.create_matrix 4 4 0;;  
val m : int array array = [[|0; 0; 0; 0|]; [|0; 0; 0; 0|]; [|0; 0; 0; 0|]; [|0; 0; 0; 0|]]  
# for i=0 to 3 do m.(i).(i) <- 1; done;;  
- : unit = ()  
# m;;  
- : int array array = [[|1; 0; 0; 0|]; [|0; 1; 0; 0|]; [|0; 0; 1; 0|]; [|0; 0; 0; 1|]]  
# m.(1);;  
- : int array = [|0; 1; 0; 0|]
```

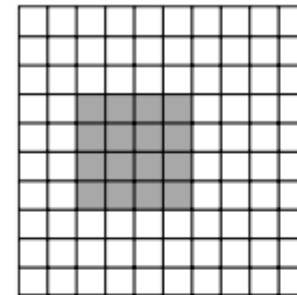
Operations on matrices

```
# let add_mat a b =  
  let r = Array.create_matrix n m 0.0 in  
    for i = 0 to (n-1) do  
      for j = 0 to (m-1) do  
        r.(i).(j) <- a.(i).(j) +. b.(i).(j)  
      done  
    done ; r;;  
  
val add_mat : float array array -> float array array -> float array array = <fun>  
# a.(0).(0) <- 1.0; a.(1).(1) <- 2.0; a.(2).(2) <- 3.0;;  
- : unit = ()  
# b.(0).(2) <- 1.0; b.(1).(1) <- 2.0; b.(2).(0) <- 3.0;;  
- : unit = ()  
# add_mat a b;;  
- : float array array = [[|1.; 0.; 1.|]; [|0.; 4.; 0.|]; [|3.; 0.; 3.|]]
```

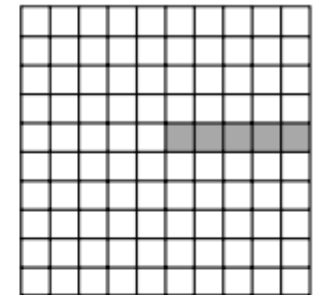
Matrices

- Multidimensional arrays
 - Declaration
 - Arrays of arrays
 - C, C++, ML, Java
 - Two-dimensional array
 - One block of memory
 - Ada, Fortran
- Slices
 - A slice is a rectangular portion of an array.
 - R, Fortran, Python

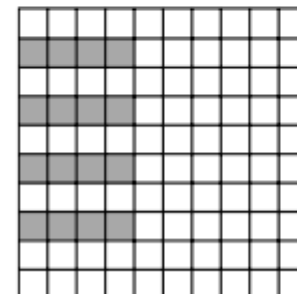
```
/* C */  
double mat[10][10];  
/* Ocaml */  
type 'a matrix = array array 'a;;  
/* Modula-3 */  
VAR mat : ARRAY [1..10] OF ARRAY [1..10] OF REAL;  
/* Ada */  
mat1 : array (1..10, 1..10) of real;
```



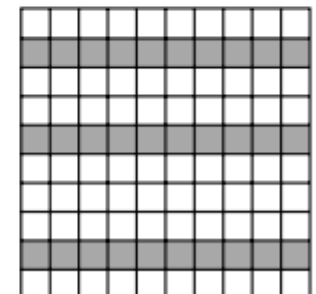
matrix(3:6, 4:7)



matrix(6:, 5)



matrix(:, 2:5)



matrix(1:2, 5, 9:10)

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Sets

- A set stores unique values, without any particular order
- Basic operations
 - Set ops: create, delete, add_element, delete_element
 - Boolean ops: membership, subset, equality, disjoint
 - Set algebra: union, difference, intersection
- Implementation
 - There are many different ways of implementing sets
 - Each with serious weaknesses for some purposes
 - For any specific purpose, it is not hard to implement set functionality using commonly available data structures

Sets

- Implementation
 - Lists, arrays (unefficient)
 - Bitstrings (storage efficient, converted to instructions)
 - Binary search trees (library: Ocaml, Haskell)
 - Hash tables
 - Dictionary representation of sets
- Sets in programming languages
 - Libraries: C++, Java, .NET, Ruby, Ocaml, Swift, Erlang
 - Build-in: Javascript, Python, Pascal

Sets in Python

- Examples:

```
thisset = {"apple", "banana", "cherry"}

for x in thisset:
    print(x)

thisset.add("orange")
thisset.remove("banana")
thisset.discard("banana") # not  $\exists$  -> no error
del thisset               # delete complete set

set2 = {1, 2, 3}
set3 = set1.union(set2)   # {3, 'b', 'a', 2, 1, 'c'}
```

Sets in Python

- `add()` Adds an element to the set
- `remove()` Removes the specified element
- `discard()` Remove the specified item
- `pop()` Removes an element from the set
- `clear()` Removes all the elements from the set
- `copy()` Returns a copy of the set
- `union()` Return a set containing the union of sets
- `intersection()` Returns a set, that is the intersection of two other sets
- `difference()` Returns a set contains the difference betw two or more sets
- `isdisjoint()` Returns whether two sets have a intersection or not
- `Issubset()` Returns whether another set contains this set or not
- `issuperset()` Returns whether this set contains another set or not
-
- ... and more

Unions

- Type constructed by union
 - Make a new type by taking the union of existing types
- Unions in Ocaml
 - Type definition
 - Construction of instance
 - Pattern matching
- Union in other languages
 - Tagged union:
 - ML-family, Haskell
 - Pascal, Ada, Modula2
 - Also called: Variant records in Pascal
 - Untagged union: C, C++

```
type name = ...  
  | Namei ...  
  | Namej of tj ...  
  | Namek of tk * ... * tl ... ;;
```

Unions in C

- Type that allows multiple different values to be stored in the same memory space
 - Size = the largest component

```
union Data {  
    int i;  
    float f;  
    char str[20];  
} data;
```

```
union [union tag] {  
    member definition;  
    member definition;  
    ...  
    member definition;  
} [one or more union variables];
```

```
int main( ) {  
    union Data data;  
    data.i = 10;  
    data.f = 220.5;  
    strcpy( data.str, "C Programming");  
    printf( "data.i : %d\n", data.i);  
    printf( "data.f : %f\n", data.f);  
    printf( "data.str : %s\n", data.str);  
    return 0;  
}
```

Variant records in Pascal

- Parts of records are variant
 - Type tag is used to differentiate among the variants
 - Records must include the largest variant

```
type paytype=(salaried, hourly);
var employee: record
    id: integer;
    dept: array [1...3] of char;
    age: integer;
    case payclass: paytype of
        salaried: (monthlrate: real; stardate: integer);
        hourly: (hourrate: real; reghours: integer; overtime: integer);
    end;
```

Dictionaries

- Alternative names
 - Associative array, map, symbol table
- A store of key/value pairs
 - Keys and values are of arbitrary type
 - Operations provided
 - Create, access, update, delete, to-list, keys, ...
- Programming languages
 - Initial implementations
 - TMG (1965, compiler-compiler), SETL (late 1960s), Snobol (1969)
 - Script languages
 - AWK, Rexx, Perl, PHP, Tcl, JavaScript, Python, Ruby, Go, Lua

Dictionaries

- Other languages
 - C++, Java, Scala, Erlang, OCaml, Haskell
- Implementation of a dictionary
 - Hash tables
 - $O(1)$
 - Search trees
 - Binary search trees, B+-trees, ...
- Very popular and useful data structure
 - Any data structure can be represented

Python dictionary operation

- Creation
 - `D = {}`, `D = {'key1':value1, 'key2':value2, ... }`
 - `dict(name1=value1, name2=value2, ...)`
 - From a list: of pairs, names, ...
- Access by a key
 - `D['name']`, `D['name1']['name2']`, `'name' in D`
 - `D.get(key)`
- Update and delete a key
 - `D.update(D1)`
 - `del D[key]`, `D.pop(key)`
- Reading keys, values and key/value pairs
 - `D.keys()`, `D.values()`, `D.items()`